

Spatial Coherence in Near-Field Raman Scattering

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Inelastic light scattering in crystals has historically been treated as a spatially incoherent process, giving rise to incoherent optical radiation. Here we demonstrate that Raman scattering can be spatially coherent, in which case it depends on the dimensionality and symmetry of the scatterer. Using near-field spectroscopy, we measure a correlation length of ~ 30 nm for the optical phonons in graphene, the results varying with vibrational symmetries and spatial confinement of the phonons.

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In classical textbooks inelastic scattering, such as Raman scattering, is usually treated as a spatially incoherent process, that is, the response from different volume elements are added up [1,2]. Thus, the scattered fields from spatially distinct locations are considered to be uncorrelated, and the scattered signal, S , is then proportional to the volume of the scatterer, V . This is represented by the expression $S \propto V |\mathbf{e} \cdot \vec{\alpha} \mathbf{E}|^2$, where \mathbf{e} is a unit vector defining the scattering polarization direction and $\vec{\alpha}$ is the polarizability of a volume element [1,2]. This formalism has been justified for macroscopic light-matter interactions because the correlation length L_c of material excitations, such as optical phonons, is typically on the order of tens of nanometers, one order of magnitude shorter than the wavelength of visible light. However, while correlation lengths significantly smaller than the wavelength λ are inaccessible in standard diffraction limited measurement schemes [3], they do play an important role in the near-field regime and cannot be neglected for scattering processes at the nanoscale [4–9]. Therefore, applications in nanotechnology demand quantitative knowledge of the correlation length of material excitations and the associated coherent properties of scattered light.

The scattered signal S at the location of the detector \mathbf{r}_0 from a material represented by a distribution of scattering dipoles \mathbf{p} is calculated by [26]

$$\begin{aligned} S(\mathbf{r}_0) &\propto \langle \mathbf{E}_S^*(\mathbf{r}_0) \mathbf{E}_S(\mathbf{r}_0) \rangle \\ &= \int \int \vec{\mathbf{G}}^*(\mathbf{r}_0, \mathbf{r}_1) \vec{\mathbf{G}}(\mathbf{r}_0, \mathbf{r}_2) \langle \mathbf{p}^*(\mathbf{r}_1) \mathbf{p}(\mathbf{r}_2) \rangle d^3 \mathbf{r}_1 d^3 \mathbf{r}_2 \\ &= \int \int \langle \vec{\alpha}_{\mathbf{r}_1}^* \vec{\alpha}_{\mathbf{r}_2} \rangle [\vec{\mathbf{G}}(\mathbf{r}_0, \mathbf{r}_1) \mathbf{E}(\mathbf{r}_1)]^* \\ &\quad \times [\vec{\mathbf{G}}(\mathbf{r}_0, \mathbf{r}_2) \mathbf{E}(\mathbf{r}_2)] d^3 \mathbf{r}_1 d^3 \mathbf{r}_2, \end{aligned} \quad (1)$$

where $\vec{\mathbf{G}}$ is the Green's tensor and $\vec{\alpha}_{\mathbf{r}_i}$ is the polarizability tensor at location \mathbf{r}_i . We consider a linear relationship

($\mathbf{p} = \vec{\alpha} \mathbf{E}$) between dipole and local field. The expression $\langle \vec{\alpha}_{\mathbf{r}_1}^* \vec{\alpha}_{\mathbf{r}_2} \rangle$ accounts for the correlation between scattering dipoles \mathbf{p} at positions \mathbf{r}_1 and \mathbf{r}_2 . If the correlation length is negligible, the correlation function is a Dirac delta function $\delta(\mathbf{r}_1 - \mathbf{r}_2)$. As a consequence, the spatial coherence of scattered light is low. However, if the light-matter interaction volume becomes comparable to the correlation length we can no longer approximate $\langle \vec{\alpha}_{\mathbf{r}_1}^* \vec{\alpha}_{\mathbf{r}_2} \rangle$ by a delta function. Here we use a near-field Raman scattering scheme to experimentally demonstrate the importance of the correlation function $\langle \vec{\alpha}_{\mathbf{r}_1}^* \vec{\alpha}_{\mathbf{r}_2} \rangle$ in the scattered intensity. Using strongly localized light fields, we measure phonon correlation lengths in graphene of 30 ± 5 nm, which is more than an order of magnitude smaller than the excitation wavelength. Furthermore, we find that the spatial coherence of scattered light is strongly influenced by the symmetry of the phonon mode involved in the scattering process. The spatial coherence of phonons is of great importance for graphene electronics and has so far only been explored in the time and frequency domains [10–15]. Near-field Raman scattering can also be used to measure phonon correlations in polycrystalline and noncrystalline solids, where the correlation lengths are significantly shorter than in crystals. This opens new research directions for tip-enhanced Raman spectroscopy (TERS).

For a coherent process the strength of the scattered field depends on the symmetry of the vibrational mode, since the scattered fields from neighboring lattice points add constructively or destructively depending on the relative phase between the points. Beyond this, the dimensionality of the sample is also important since it determines the number of lattice points that are coherently added. The degree to which the fields from neighboring points interfere is determined by a spatial correlation function. Graphene is an excellent prototype material to study such correlations. Its three main Raman features span the different mode

symmetries and dimensionalities that are needed: the G ($\sim 1580\text{ cm}^{-1}$) and G' band (also called 2D, centered at $\sim 2700\text{ cm}^{-1}$) are allowed over the whole graphene lattice but they exhibit different symmetries [16,17]. The G band belongs to the E_{2g} irreducible representation in group theory, which means it is symmetric under a C_2 axis (180° rotation) [16]. The G' band belongs to the totally symmetric irreducible representation A'_1 , thus exhibiting the full C_6 (60° rotation) symmetry of graphene [16]. The third prominent band is the defect-induced D band ($\sim 1350\text{ cm}^{-1}$), which is highly localized at graphene edges [18–21]. This Raman feature has the same symmetry as its overtone G' band, but unlike the two previous cases that are spread over the two-dimensional (2D) graphene lattice, the localization of the D band mimics a one-dimensional (1D) system. Therefore, graphene allows us to study the spatial coherence of the Raman process for different mode symmetries and dimensionalities.

Our experiments were performed with a near-field Raman microscope, as described in Refs. [22,23]. Figure 1(a) illustrates the measurement scheme and Fig. 1(b) shows a typical TERS image (G') of a single-layer graphene flake. As a comparison, the inset shows the confocal image of the same area of the flake. These images

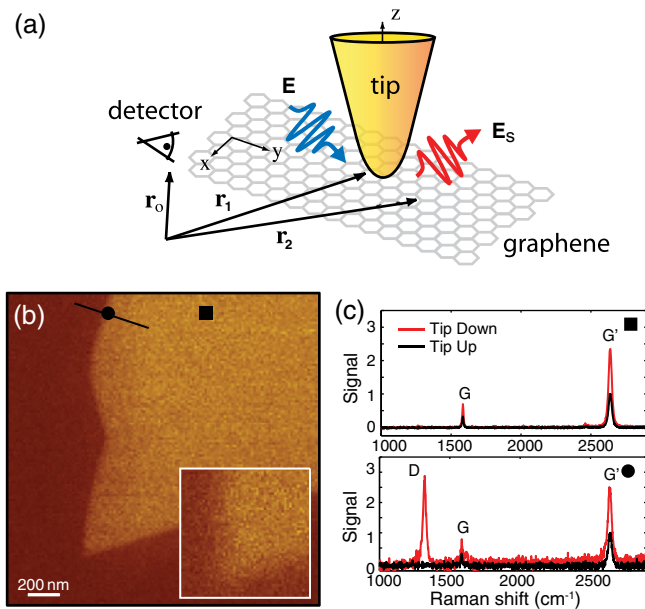


FIG. 1 (color online). TERS characterization of a graphene flake. (a) Sketch of the experiment. An incident electric field, \mathbf{E} , inelastically scatters off the graphene lattice creating the outgoing field \mathbf{E}_s . A gold tip is used to measure the correlations on the sample. (b) TERS image of the G' band of a single graphene flake. The black line indicates the location of the hyperspectral line scan in Fig. 2. Inset: confocal image of the same area with the color contrast scaled by $\times 3$. (c) Raman spectra with (red) and without (black) the tip acquired in the center (top panel) and at the edge (bottom panel) of the flake. The locations are indicated by the black square and circle in (b), respectively.

clearly show the improvement in signal and resolution in the near-field configuration. To better illustrate the TERS enhancement, spectra were acquired at the edge [black circle in Fig. 1(b)] and in the center of the flake [black square in Fig. 1(b)] with the tip down (red) and retracted (black), which are shown in top and bottom panels of Fig. 1(c), respectively. We do not observe any disorder-induced D band away from the edge, indicating that the flake is pristine.

In order to further study the TERS signal, hyperspectral line scans were acquired with and without the tip. In this case, the sample was scanned along a line perpendicular to the edge and at each spatial position a spectrum was acquired [Fig. 2(a)]. The resulting spectra were fit with Lorentzians and normalized by the tip-up values at each location. Figure 2(b) shows the results for the D band, indicating that the D band signal is greatly enhanced and highly localized at the edge to $\sim 40\text{ nm}$. This provides a measurement of the tip radius, $r_{\text{tip}} \approx 18 \pm 3\text{ nm}$. The width of the D band intensity profile is slightly larger than $2r_{\text{tip}}$, due to a convolution of the near-field spot with the spatial extent of the D band ($\approx 4\text{ nm}$). The latter corresponds to the distance from the graphene edge for which the D band is still Raman active and is determined by the coherence length (or phase-breaking length) of the excited electronic

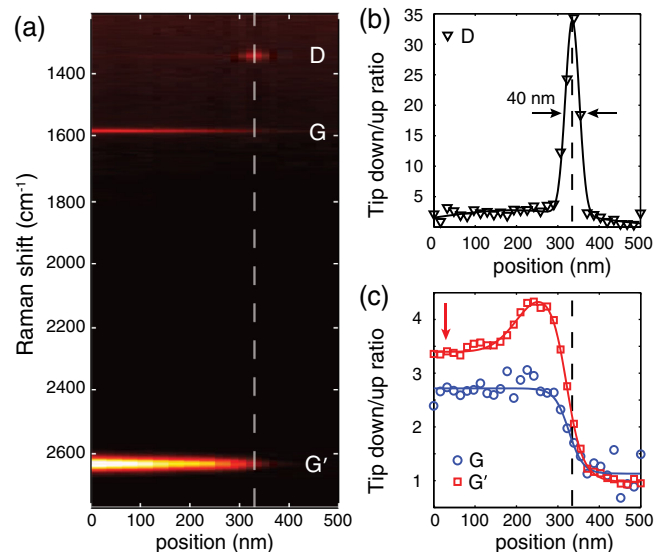


FIG. 2 (color online). TERS hyperspectral line scan acquired along the black line in Fig. 1(b). (a) Color map showing the intensities of the Raman bands as one moves from the inside (position equals 0 nm) to the outside of the flake (position equals 500 nm). The edge of the flake is indicated by the dashed line. (b), (c) Plots of the amplitudes for the D (black triangles), G (blue circles), and G' (red squares) bands from the hyperspectral line scan shown in (a). The tip-down spectra are normalized by the far-field value at each location. The D band profile is fit with two Gaussians: one for the confocal focus and one for the near-field signal. The bump near the edge in the G' band data is likely due to strain and dopants.

states [18–21]. The line scans of the G and G' bands look similar, being more intense when the near-field of the tip enters the graphene material, as shown in Fig. 2(c). However, there are important differences: the G' band shows a steeper signal increase at the graphene edge. Furthermore, away from the edge (red arrow), the measured enhancement for the G' band is larger than for the G band. The reduced enhancement of the G band compared to the G' band, together with the different signal steepness at the edge, provides evidence that both the spatial phonon correlations and the phonon mode symmetry impact the TERS signal.

The results in Fig. 2 demonstrate qualitatively that mode confinement and symmetry are important in Raman scattering. For a more quantitative analysis, the dependence of the Raman enhancement on the phonon correlation length should be studied as a function of the tip-sample separation. The theoretical dependence of the signal on the tip-sample separation (z_{ts}) is summarized in Fig. 3 for the D , G , and G' bands. The theoretical results are an extension of Refs. [24,25] and are described in detail in Ref. [26]. The D band signal is evaluated at the graphene edge, whereas the G and G' bands are evaluated in the interior of the flake. Figures 3(a) and 3(b) show tip-sample distance curves for two values of the phonon correlation length L_c : 0 and 50 nm, respectively. In the case of a spatially uncorrelated

process ($L_c = 0$), the G and G' curves coincide [Fig. 3(a)]. However, due to the different dimensionality of the scattering domain (edge versus interior), the D band has a steeper tip-sample distance dependence (stronger enhancement). The distance dependence drops for all bands as L_c increases [Fig. 3(b)]. Most importantly, as L_c increases the G and G' signals become strikingly different, with the G band showing a markedly weaker enhancement. Note that the D and G' bands are both second-order scattering processes. Their excited electron-hole pairs are spatially confined to a few nanometers [19–21], which does not influence the phonon correlations measured in this work.

The deviation between the G and G' bands arises from the interaction between neighboring lattice points and provides theoretical evidence for interference effects associated with the coherence of the scattered field. This interference is illustrated in sketches of the TERS process shown in Figs. 3(c) and 3(d). The incident field (vertical black arrow) induces a vertical dipole in the tip. The fields from the tip induce dipoles in the sample (horizontal arrows), which then interact again with the tip by inducing a vertical dipole (at the Raman frequency) that scatters the Raman signal to the detector. The strength of the Raman signal depends on the relative phase of the dipoles induced in the sample. For the G' band the fields from the dipoles in the sample add constructively at the tip [Fig. 3(c)]. However, for the G band the fields destructively interfere, which reduces the Raman signal at the detector [Fig. 3(d)]. These theoretical curves indicate how nanoscale spatial correlations can be experimentally determined by measuring the distance dependence of the TERS signal.

To experimentally validate the theoretical predictions, we have measured the tip-sample distance dependence of three different Raman modes in graphene. The tip was positioned over the edge of a graphene flake and was retracted from the surface while Raman spectra were acquired for discrete tip-sample separations z_{ts} . The data were fit using Eq. (1), which was theoretically developed in Ref. [26]. The fitting parameters are the phonon correlation length L_c and the field enhancement factor f_e . The latter depends solely on the plasmonic properties of the tip. For the G' band f_e primarily determines the steepness of the curve in the last 10–20 nm, whereas L_c strongly influences larger tip-sample separations. However, the G band is very sensitive to L_c even for short tip-sample separations due to the destructive interference at the tip. Figure 4(a) shows the approach curves for the D (black triangles), G (blue circles), and G' (red squares) bands. From the fits we find $L_c = 30 \pm 5$ nm and $f_e = 4.0$. r_{tip} was independently determined from the spatial confinement of the D band. The enhancement is clearly more modest for the G band than for the G' or D band, as expected due to the interference effect discussed above. The differences in the approach curves for distinct bands are better shown by

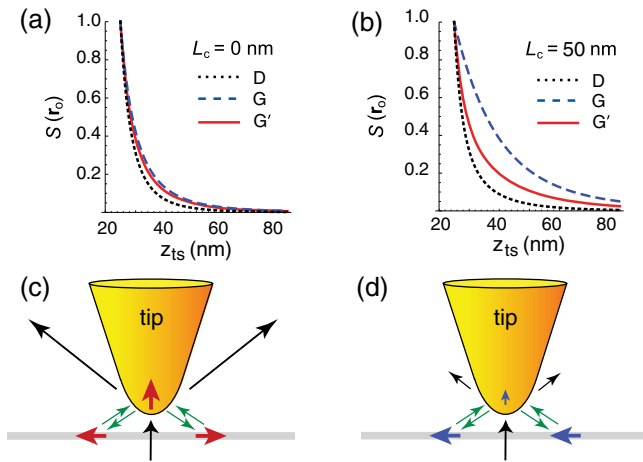


FIG. 3 (color online). Theoretical description of the TERS signal. (a),(b) Dependence of the signal on the tip-sample separation (z_{ts}) for the D , G , and G' bands. The curves are calculated with two different phonon correlation lengths: $L_c = 0$ nm and $L_c = 50$ nm. The signal $S(r_0)$ is normalized to 1 for $z_{ts} = 25$ nm, which corresponds to the closest tip-sample distance. (c),(d) Sketches of the TERS process. The incident field induces a vertical dipole in the tip that interacts with the sample (green arrows), which in turn acts back on the tip at the Raman frequency (green arrows) before the fields are scattered out to the detector. The strength of the scattered signal depends on the relative phase of the induced dipoles in the sample (horizontal red and blue arrows). The emission dipoles on the sample add constructively for the G' band and destructively for the G band, as shown in (c),(d), respectively.

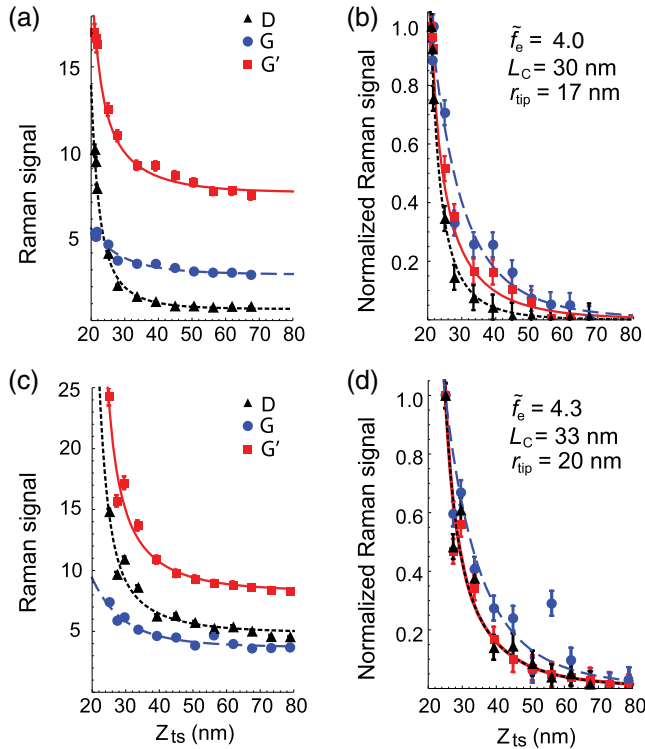


FIG. 4 (color online). Experimental tip-sample distance curves for the Raman D (black triangles), G (blue circles), and G' (red squares) bands of two graphene samples. Top row: acquired at the edge of a pristine graphene flake. Bottom row: ion bombarded flake with uniformly distributed defects. (a),(c) Amplitudes of the Raman bands. (b),(d) Normalized data from (a) and (b), respectively, with the far-field values subtracted. The data are overlaid with the theoretical curves evaluated in Ref. [26], and shown Fig. 3. The values for the enhancement factor (\tilde{f}_e), correlation length (L_c), and tip radius (r_{tip}) are indicated in the plots.

subtracting the far-field value (signal in absence of the tip) before normalizing, as shown in Fig. 4(b). The results clearly demonstrate that the D band has a stronger tip-sample distance dependence than the G and G' bands, and this difference is due to the fact that the edge behaves as a 1D scatterer. Furthermore, the G' band enhancement is stronger than for the G band for finite values of L_c , which is clearly seen in the measurement shown in Fig. 4(b). Note that we are measuring the phonon correlation length using the coherence properties of the Raman signal and we do not need to directly resolve L_c . However the size of the tip does influence the measurements. Each correlated area, A_c , on the sample has a well-defined phase, but the phase is random between different regions. As the tip size increases it interacts with a larger sample area and the degree of coherence depends on the number of A_c areas that are averaged (see the Supplemental Material [27]).

To further distinguish the roles of the mode symmetry versus sample dimensionality on the TERS signal, a defective flake was prepared by ion bombardment with an interdefect spacing of ~ 15 nm [19]. In this case, the D

band is active everywhere on the 2D flake and no longer confined to the 1D edge. We acquired an approach curve in the center of this graphene flake and the results are shown in Figs. 4(c) and 4(d). It is evident that the enhancement for the D and G' bands is stronger than for the G band [Fig. 4(d)]. In addition, the approach curves for the D and G' bands are nearly identical. As discussed earlier the D and G' bands have A'_1 symmetry, whereas the G band has E_{2g} symmetry. These results clearly show that the phonon symmetry significantly influences the near-field signal. From the fitting procedure, we find $L_c = 33 \pm 5$ nm and $\tilde{f}_e = 4.3$ for this data set, which is in good agreement with the measurement at the edge [Figs. 4(a) and 4(b)]. The similar values for L_c at the edge and away from the edge indicate that the phonon-edge scattering is not affecting the spatial coherence (see the Supplemental Material [27]).

Although coherence effects in inelastic light scattering have been neglected for decades, we find that near-field Raman scattering must be treated as a partially coherent process and that it is highly sensitive to the dimensionality and symmetry of the scatterer. While the importance of Raman spectroscopy for studying and characterizing nanostructures is well established [16,17], we demonstrate that this technique also provides access to spatial correlation functions, such as phonon coherence lengths. Recent studies have shown TERS with spatial resolutions of better than 1 nm [28,29], which brings TERS resolutions to the level of scanning tunneling microscopy. At this length scale coherence effects will completely dominate the measured signals in extended material systems. Furthermore, this technique opens the possibility of exploring the impacts of the substrate, carrier concentration, defect density, and temperature on phonon correlations.

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